

FINM 36700 - Midterm Exam

Portfolio and Risk Management

Winter 2026

- This exam contains 100 multiple choice questions.
- Questions marked with [†] are [**Select All That Apply**] – they may have zero, one, or multiple correct answers.
- No calculators or computers are allowed.
- All calculations are designed for mental math.

Section 1: Mean-Variance Optimization

Questions 1–3: Three-Asset Snapshot

Reference Table: Expected returns and volatilities

Asset	$E[r]$	σ	Notes
A	6%	10%	$\text{Corr}(A, B) = 0$
B	8%	20%	$\text{Corr}(A, C) = 0.5$
C	10%	30%	$\text{Corr}(B, C) = 0.5$

- A portfolio invests 50% in A and 50% in B. What is its expected return?
 - 6%
 - 7%
 - 8%
 - 9%
- Using $\text{Corr}(A, B) = 0$, what is the approximate volatility of the 50/50 A–B portfolio?
 - 10%
 - 11%
 - 14%
 - 20%
- Which pair offers the strongest diversification benefit based on correlations?
 - A and B
 - A and C
 - B and C
 - All pairs are equally diversifying
- † [Select All That Apply] Which statements about the efficient frontier with a risk-free asset are correct?
 - ☐ The tangency portfolio maximizes the Sharpe ratio among risky portfolios.
 - ☐ Adding a new asset cannot reduce the maximum achievable Sharpe ratio.
 - ☐ The tangency portfolio must include every risky asset with positive weight.
 - ☐ The capital market line is unchanged if expected returns all rise by the same constant.
- If the covariance matrix is assumed diagonal (all correlations set to zero), the MV optimal weights are proportional to:
 - $1/\sigma$
 - μ/σ^2

- μ/σ
 - σ/μ
6. For a large N -asset portfolio with identical variances and average pairwise correlation ρ , the limiting portfolio variance as $N \rightarrow \infty$ is approximately:
- 0 for any $\rho < 1$
 - σ^2/N
 - $\rho\sigma^2$
 - σ^2 regardless of ρ
7. If the correlation between two assets in a portfolio decreases while their individual volatilities and expected returns remain constant, the portfolio's Sharpe Ratio will generally:
- Increase.
 - Decrease.
 - Remain exactly the same.
 - Become negative.
8. In a MV-efficient world, what is the slope of the Capital Market Line?
- Sharpe ratio of market portfolio
 - Mean return of market portfolio
 - Risk-free rate
 - Treynor ratio of market portfolio
9. In portfolio optimization, measurement error is most problematic for:
- Transaction costs.
 - Expected returns.
 - Covariances.
 - The risk-free rate.
10. Suppose all assets have identical Sharpe ratios and volatility but varying correlations. Which of the following is true of the tangency portfolio?
- The tangency portfolio is any portfolio with positive weights summing to 1.
 - The tangency portfolio is undefined.
 - Any mean-variance efficient portfolio of risky assets becomes a tangency portfolio.
 - The tangency portfolio reduces to the global minimum variance (GMV) portfolio.
11. Consider the Two-Fund Separation Theorem. If the borrowing rate r_{borrow} is higher than the lending rate r_{lend} , how many tangency portfolios exist?
- Still exactly one unique tangency portfolio.
 - Two distinct tangency portfolios (one for each rate)
 - Infinitely many tangency portfolios
 - The efficient frontier ceases to be convex.

Question 12: Gross Exposure Constraint

Reference Table: Unconstrained MVO weights

Asset	Weight	μ (Expected Return)	σ (Volatility)
AAPL	+240%	15%	32%
NVDA	+180%	18%	45%
SPY	-320%	10%	16%
Portfolio	100%	24.4%	28.1%

12. If you add a **gross exposure constraint of 200%** (weights sum to 100%), approximate new weights are:
- AAPL = 120%, NVDA = 90%, SPY = -110%
 - Weights scale proportionally to original ratios
 - AAPL = 80%, NVDA = 60%, SPY = -40%
 - AAPL = 80%, NVDA = 70%, SPY = -50% (sums to 100%, gross = 200%)
13. A constraint has a positive Lagrange multiplier at the optimum. This indicates that:
- The optimization is infeasible
 - Relaxing the constraint would improve the objective
 - The constraint is slack and irrelevant
 - The constraint lowers portfolio variance at no cost
14. A long-only constraint forces an asset with negative unconstrained weight to:
- An indeterminate weight
 - Zero weight in the constrained solution
 - Positive weight in the constrained solution
 - Negative weight with reduced magnitude
15. [†] **[Select All That Apply]** Which inputs are most likely to make MV weights unstable?
- ☐ Highly correlated assets (ill-conditioned covariance matrix)
 - ☐ Noisy expected-return estimates
 - ☐ Increasing sample size for estimating covariances
 - ☐ Imposing long-only constraints

Section 2: Harvard Endowment Case (HW1)

Questions 16–25: HMC Asset Allocation

Background: Harvard Management Company (HMC) manages a multi-billion dollar endowment across 11 asset classes. They use a two-stage optimization process and place bounds on allocations rather than implementing unconstrained MV solutions.

Reference Table: Selected HMC Asset Class Statistics (Annualized)

Asset Class	Mean	Vol	Sharpe	Corr w/ Dom Eq	Weight (Bounded)
Domestic Equity	12%	16%	0.50	1.00	0%
Foreign Equity	10%	20%	0.35	0.60	15%
Private Equity	16%	24%	0.50	0.40	15%
Domestic Bonds	4%	8%	0.25	0.20	0%
TIPS	3%	6%	0.17	0.10	5%
Commodities	6%	20%	0.15	−0.10	10%
Real Estate	8%	12%	0.42	0.30	10%

16. [†] **[Select All That Apply]** Why does HMC use a two-stage optimization (first within asset classes, then across asset classes) rather than optimizing across all individual securities directly?
- ☐ Estimation error in the covariance matrix becomes severe with thousands of securities.
 - ☐ The number of parameters to estimate grows as $N(N + 1)/2$, creating dimensionality problems.
 - ☐ Regulatory requirements mandate asset-class-level reporting.
 - ☐ Two-stage optimization always produces higher Sharpe ratios than single-stage.
17. In the HMC data, if we drop TIPS from the investment set entirely, the tangency portfolio's Sharpe ratio will:
- Stay exactly the same, because TIPS have near-zero correlation with equities.
 - Become undefined, because TIPS are needed to span the efficient frontier.
 - Increase, because TIPS have the lowest Sharpe ratio.
 - Decrease or stay the same, because removing an asset cannot expand the opportunity set.
18. HMC focuses on **real** (inflation-adjusted) returns rather than nominal returns. This matters for MV optimization because:
- Real returns are always higher than nominal returns.
 - Real returns have lower volatility than nominal returns.
 - Inflation affects asset classes differently, changing both correlations and relative expected returns.
 - MV optimization requires returns to be expressed in real terms by construction.

19. [†] [Select All That Apply] Commodities have a low Sharpe ratio (0.15) but receive 10% weight in the bounded portfolio. Which reasons could justify this allocation?
- ☐ Commodities have negative correlation with Domestic Equity, providing diversification.
 - ☐ Commodities have the highest expected return in the table.
 - ☐ Adding a low-correlation asset can improve portfolio Sharpe even if its standalone Sharpe is low.
 - ☐ The bounded optimization requires at least 10% in each asset class.
20. In the Constrained Optimization homework, weights were bounded between -10% and $+20\%$ per position. If the unconstrained weight for NVDA was $+180\%$, what would happen to NVDA's weight in the bounded solution?
- It would be exactly $+20\%$, hitting the upper bound.
 - It would be $+100\%$, the maximum allowed for any single position.
 - It would be 0% , because extreme weights are eliminated.
 - It would be $+90\%$, half of the unconstrained value.
21. A fund has $R^2 = 0.85$ in a regression on market factors. What percentage of the fund's return variance is **idiosyncratic** (not explained by the factors)?
- 0%
 - 15%
 - 85%
 - Cannot determine from R^2 alone
22. Based on the HMC table, which asset provides the strongest diversification benefit relative to Domestic Equity?
- Private Equity
 - Commodities
 - Foreign Equity
 - Real Estate
23. A constrained optimizer shows Lagrange multipliers for policy bounds below. Which bound is most costly?

Constraint	Lagrange Multiplier
Domestic Equity $\leq 30\%$	0.2
Private Equity $\leq 15\%$	1.1
Real Estate $\leq 10\%$	0.4

- Private Equity bound
- Real Estate bound
- All equal
- Domestic Equity bound

24. Two portfolios have the following characteristics (risk-free rate 4%):

Portfolio	$E[r]$	σ
P1	10%	12%
P2	14%	20%

Which portfolio has the higher Sharpe ratio?

- P1
- P2
- Equal
- Cannot be determined

25. [†] **[Select All That Apply]** Why might an investment policy committee impose upper bounds on asset class weights even when the optimizer wants higher allocations?

- ☐ Liquidity constraints for large endowments
- ☐ Estimation error makes extreme optimal weights unreliable
- ☐ Governance and fiduciary responsibility concerns
- ☐ Upper bounds always improve the portfolio Sharpe ratio

Section 3: Linear Factor Decomposition

Questions 26–36: Factor Regression

Reference Table: Monthly factor regressions

Fund	β_{Mkt}	β_{Bond}	α (ann.)	R^2	TE
Fund A	0.6	0.2	1.0%	0.80	4%
Fund B	1.0	-0.1	0.0%	0.40	8%
Fund C	0.3	0.5	2.0%	0.55	6%

26. Which fund has the highest tracking error?

- Fund C
- All equal
- Fund A
- Fund B

27. In a Linear Factor Decomposition (LFD) regression $R_p = \alpha + \beta_1 F_1 + \beta_2 F_2 + \epsilon$, if we want to build a *tradeable* replication of R_p using ETFs for F_1 and F_2 , we should probably:

- Ignore the betas and just equal weight the ETFs.
- Short the ETFs to capture the alpha.
- Focus on maximizing the R^2 including the intercept.
- Force the intercept to zero.

28. In a replication context, basis risk refers to:

- The risk that the hedge fund manager changes the strategy.
- The risk that we cannot replicate the fund exactly due to differences in strategy.
- The volatility of the tracking error between the replication and the target.
- The risk of interest rates rising.

29. [†] **[Select All That Apply]** Which statements about a “Time-Series Regression” (regressing one asset’s returns on factor returns over time) are correct?

- ☐ It estimates the factor loadings (β s) of a specific asset.
- ☐ It can be used to test whether alpha is statistically different from zero.
- ☐ It estimates the risk premiums (λ) of factors across many assets.
- ☐ It directly proves that mean-return estimates are accurate.

30. [†] **[Select All That Apply]** Which statements about multicollinearity are correct?

- ☐ Betas can become unstable across samples
- ☐ Individual t-stats can be small even if R^2 is high

- ☐ Multicollinearity guarantees low R^2
- ☐ Multicollinearity eliminates tracking error
31. You estimate the regression $r_{NVDA} = \alpha + \beta r_{Mkt} + \epsilon$ and find $\alpha = 2\%$ (annualized). If you go long NVDA and short β units of the market, what is the expected excess return of this hedged position?
- β times the market risk premium.
 - The tracking error of the regression.
 - Zero, because the market exposure is hedged out.
 - Approximately α (2%), the portion of mean return not explained by the market.
32. [†] **[Select All That Apply]** A PM asks if EAFE Dividend (Div) offers any advantage over EAFE Value (Val) for understanding a fund's monthly excess returns. Which study designs constitute a rigorous test of Div's incremental value over Val?
- ☐ Regress the fund on EAFE Market, Val, and Div (all investable total-return series), including an intercept, assess whether Div's partial slope is significant and stable out-of-sample
- ☐ Before the LFD, orthogonalize Div with respect to Val within the EAFE and then test if the orthogonal Div reduces Tracking Error and improves stability.
- ☐ Omit EAFE Market and compare in-sample R^2 between {Val} and {Val, Div}. Higher R^2 for the latter proves Div's advantage.
- ☐ Whichever of Val or Div correlates more with the fund (pairwise) is the better descriptor.
33. For a replication using only tradable assets of a target using liquid factors, which estimation choice is most consistent with the goal?
- Omit the intercept as it is not investible, accept lower R^2 , and control tracking error.
 - Include the intercept to maximize in-sample R^2 . The intercept can be purchased as a cash sleeve.
 - Include the intercept so the replication is guaranteed to have non-zero alpha out-of-sample.
 - Either way is identical for out-of-sample tracking error.
34. A team argues: "Our replication corr = 0.90 to the target, so tracking error is negligible." The best response is:
- No, high correlation measures co-movement of changes, but level drift and volatility differences still create material tracking error.
 - Yes, corr ≥ 0.90 implies tracking error <10% by definition.
 - No, high corr guarantees negative alpha.
 - Yes, corr ≥ 0.90 implies we matched all moments.
35. [†] **[Select All That Apply]** Fund A trails its benchmark by exactly 1% every year (due to fees), while Fund B averages the same 0% excess return as the benchmark but with annual deviations (sometimes +2%, sometimes -2%). Which statements are true?

- ☐ Fund A has higher tracking error than Fund B
 - ☐ Fund B has higher tracking error than Fund A
 - ☐ Both funds have the same tracking error
 - ☐ Fund A has tracking error near zero (constant underperformance is not volatility)
36. Fund X and Fund Y are managed identically, except Fund Y uses $2\times$ leverage on every position compared to Fund X. Fund X's information ratio is 0.5. What will be Fund Y's information ratio?
- 0.5 (IR is scale-invariant: both alpha and tracking error double)
 - 1.0
 - 0.25
 - Cannot be determined.

Section 4: ProShares Replication Case (HW2)

Questions 37–44: Hedge Fund Replication

Background: ProShares HDG ETF attempts to replicate the HFRI hedge fund index using liquid factors. The replication uses a rolling 60-month regression to estimate factor weights.

Reference Table: Performance Comparison (Annualized, 2012–2023)

Series	Mean	Vol	Sharpe	Skew	Kurtosis	Max DD
HFRI (Target)	5.2%	5.8%	0.62	−0.8	4.5	−12%
HDG (Replication)	4.8%	6.2%	0.52	−0.6	3.8	−14%
SPY	12.4%	15.2%	0.68	−0.5	4.2	−34%

37. The term “Alternative Beta” in the ProShares case refers to:
- The beta of hedge funds relative to the S&P 500.
 - Returns from investing in alternative assets like commodities and real estate.
 - Systematic risk factor exposures that explain hedge fund returns, captured via liquid instruments.
 - The portion of hedge fund returns unexplained by any factor model.
38. † [Select All That Apply] Why does the HDG replication use a rolling 60-month window rather than the full sample for estimating factor weights?
- ☐ Hedge fund exposures may change over time as strategies evolve.
 - ☐ A rolling window guarantees higher R-squared than full-sample estimation.
 - ☐ Recent data may be more relevant for predicting near-term factor exposures.
 - ☐ Regulatory requirements mandate 60-month lookback periods for ETFs.
39. In the LFD regression for replication, why might we choose to omit the intercept (force $\alpha = 0$)?
- Including an intercept always reduces out-of-sample R-squared.
 - The intercept represents alpha, which is not tradeable or investable.
 - Omitting the intercept is required when using excess returns.
 - The intercept has no economic interpretation in factor models.
40. A fund has a positive alpha of 0.15% per month with t-stat = 1.88. At the 5% significance level (t-critical ≈ 2.0), we conclude:
- The regression is misspecified.
 - We need more factors to determine significance.
 - The fund has statistically significant alpha; the manager adds value.
 - The fund’s alpha is not statistically significant; it could be zero.
41. † [Select All That Apply] The ProShares replication showed significant tracking error in 2008 and trailed HFRI in 2012–2013. Which mechanisms could explain this?

- ☐ The 60-month rolling window creates lag in adapting to regime changes.
 - ☐ Factor exposures estimated from calm periods may not hold during crises.
 - ☐ High in-sample R-squared guarantees low out-of-sample tracking error.
 - ☐ The HFRI index methodology changed in 2012.
42. [†] **[Select All That Apply]** Investors sometimes intentionally “leave a basis” (use a partial hedge). Which reasons could explain an intentional partial hedge?
- ☐ The asset has non-hedgeable risk factors or is illiquid.
 - ☐ Shorting the exact asset or a perfect proxy is expensive or infeasible.
 - ☐ The investor wants to retain some upside exposure to the asset’s unique risks.
 - ☐ Leaving basis risk increases expected returns.
43. [†] **[Select All That Apply]** The HFRI index and HDG replication both show negative skewness and excess kurtosis relative to a normal distribution. Which implications follow?
- ☐ Tail losses are more severe than a normal distribution would suggest.
 - ☐ Normal VaR will underestimate the true downside risk.
 - ☐ The strategies must have higher Sharpe ratios than SPY.
 - ☐ VaR based on normal assumptions will overestimate risk.
44. Comparing hedge fund fees (2% management + 20% performance) to HDG’s 0.95% expense ratio: if both strategies have gross excess return of 8% and volatility of 10%, approximately how much higher is HDG’s net Sharpe ratio?
- Same; fees don’t affect Sharpe ratio.
 - About 0.10 higher.
 - About 0.25–0.30 higher.
 - About 0.50 higher.

Section 5: Value-at-Risk and Risk Measures

Questions 45–51: Ordered Returns

Reference Table: 10 daily returns (worst to best)

-5%	-4%	-3%	-2%	-1%	0%	1%	2%	3%	4%
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45. The 10% empirical VaR is:

- -5%
- -4%
- -3%
- -2%

46. The 20% empirical VaR is:

- -5%
- -4%
- -3%
- -2%

47. The 20% empirical CVaR is:

- -4.5%
- -4.0%
- -3.5%
- -5.0%

48. [†] **[Select All That Apply]** A VaR backtest shows 12% exceptions at the 5% level. This implies:

- ☐ The model is underestimating risk
- ☐ Losses are heavier-tailed than assumed
- ☐ The model is conservative
- ☐ The model has perfect calibration

49. [†] **[Select All That Apply]** If a portfolio has a return distribution with negative skewness and high kurtosis, a standard Normal VaR will likely:

- ☐ Underestimate the true risk.
- ☐ Overestimate the true risk.
- ☐ Fail to capture the fat left tail of the distribution.
- ☐ Produce fewer VaR exceedances than predicted if backtested.

50. [†] **[Select All That Apply]** When converting a 1-day normal VaR to a 10-day normal VaR using the $\sqrt{10}$ rule, we are implicitly assuming:
- ☐ Returns are serially uncorrelated (zero autocorrelation).
 - ☐ Returns are identically distributed across days.
 - ☐ Returns are perfectly correlated across days (+1).
 - ☐ Volatility changes predictably over time.
51. [†] **[Select All That Apply]** Which statements about “Parametric VaR” are correct?
- ☐ It assumes returns follow a specific distribution (e.g., normal).
 - ☐ It uses estimated parameters (mean, volatility) to compute the VaR analytically.
 - ☐ It requires no distributional assumptions because it uses historical data directly.
 - ☐ It is always more accurate than empirical VaR for fat-tailed distributions.

Questions 52–56: VaR Methodology

Reference Table: Portfolio Risk Statistics (Weekly Data)

Measure	Portfolio A	Portfolio B	Equal-Weight	Market
Mean (weekly)	0.20%	0.15%	0.18%	0.18%
Vol (weekly)	4.0%	3.0%	2.5%	2.0%
Skewness	−0.3	−1.5	−0.6	−0.4
Kurtosis	4.0	8.0	5.0	3.5
Empirical VaR (5%)	−6.0%	−8.0%	−4.5%	−3.0%
Normal VaR (5%)	−6.4%	−4.8%	−3.9%	−3.1%

52. [†] **[Select All That Apply]** For Portfolio B, the empirical VaR (−8.0%) is much worse than normal VaR (−4.8%). Which factors explain this gap?
- ☐ Portfolio B has fat tails (high kurtosis = 8).
 - ☐ Portfolio B has negative skewness (−1.5), pushing the left tail further out.
 - ☐ The normal VaR calculation used the wrong confidence level.
 - ☐ Empirical VaR is always more conservative than normal VaR regardless of distribution.
53. Autocorrelation in squared returns implies:
- Mean reversion.
 - Unconditional Heteroskedasticity.
 - Constant volatility.
 - Volatility Clustering.
54. If we were to calculate empirical VaR for a portfolio of subprime assets (rare but severe losses), we would likely:

- Underestimate risk, since extreme losses are rare but severe when they do occur.
- Overestimate risk, since extreme losses are rare but severe when they do occur.
- Get an accurate estimate if we use enough historical data.
- Get an estimate equal to normal VaR.

55. [†] **[Select All That Apply]** CVaR (Conditional VaR, or Expected Shortfall) is preferred over VaR because:

- ☐ CVaR is a coherent risk measure; VaR is not.
- ☐ CVaR tells you the average loss in the tail, not just the threshold.
- ☐ CVaR is always smaller (less negative) than VaR.
- ☐ CVaR satisfies sub-additivity: diversification cannot increase CVaR.

56. [†] **[Select All That Apply]** A VaR model with 5% threshold is backtested over 200 days. Which statements are correct?

- ☐ If the model is correct, we expect approximately 10 exceedances.
- ☐ Observing 25 exceedances would suggest the model underestimates risk.
- ☐ If the model is correct, we expect approximately 50 exceedances.
- ☐ Observing 5 exceedances would suggest the model underestimates risk.

Section 6: Barnstable and Long-Run Risk (HW3)

Questions 57–61: Probability of Underperformance

Background: Barnstable College Endowment believes stocks are safer in the long run and maintains 100% equity allocation. The case examines the probability that stocks will underperform the risk-free rate over various horizons.

Reference Data: Log Return Statistics (Annualized, 1965–1999)

	Mean (μ)	Volatility (σ)
Market (log returns)	8%	16%
Risk-free rate (log)	2%	–
Excess log return	6%	16%

Note: Sharpe Ratio of log excess returns = $6\%/16\% = 0.375$

57. The probability that stocks underperform the risk-free rate over horizon h years can be written as:

$$P(\text{underperform}) = \Phi(-\sqrt{h} \times \text{SR})$$

where Φ is the standard normal CDF and SR is the Sharpe ratio. For $h = 1$ year, using SR = 0.375, the probability is approximately:

- 25%
 - 15%
 - 50%
 - 35%
58. [†] [Select All That Apply] As the investment horizon h increases from 1 to 30 years, which statements about stocks vs the risk-free rate are correct (assuming i.i.d. returns and positive Sharpe ratio)?
- ☐ The probability of underperforming the risk-free rate decreases.
 - ☐ The probability of underperforming the risk-free rate increases.
 - ☐ The formula $P = \Phi(-\sqrt{h} \times \text{SR})$ drives probability toward zero as h grows.
 - ☐ The volatility of cumulative returns decreases with horizon.
59. The volatility of **annualized** returns over an h -year horizon (assuming i.i.d. returns) is:
- σ/\sqrt{h}
 - $\sigma \times h$
 - σ/h
 - $\sigma \times \sqrt{h}$
60. [†] [Select All That Apply] Barnstable’s belief that “stocks are safer in the long run” relies on which assumptions?

- ☐ Stock returns are approximately i.i.d. (independent across time).
 - ☐ The equity risk premium is positive and stable over time.
 - ☐ Stock returns are negatively autocorrelated (mean-reverting).
 - ☐ Volatility decreases as the investment horizon increases.
61. [†] **[Select All That Apply]** Using the 1965–1999 data, Barnstable calculated a 30-year underperformance probability of 3%, but actual returns from 2000–2024 were much lower than expected. Which explanations are valid?
- ☐ Parameter uncertainty: the true mean and Sharpe ratio may differ from historical estimates.
 - ☐ Regime changes: the equity premium in 2000–2024 may have been structurally different from 1965–1999.
 - ☐ The formula for underperformance probability is mathematically incorrect.
 - ☐ A 30-year horizon is always too short for any probability formula to apply.

Section 7: The Capital Asset Pricing Model

Questions 62–67: CAPM Fundamentals

Assume: $r_f = 2\%$, Market risk premium $E[\tilde{r}_m] = 6\%$, $\sigma_m = 20\%$

Asset	β	σ_ϵ^2 (Idio. Var)	Notes
X	0.5	0.04	
Y	1.2	0.09	

62. The expected excess return for Asset X is:

- 3%
- 6%
- 8%
- 2%

63. The expected total return for Asset Y is:

- 6.0%
- 8.0%
- 9.2%
- 10.0%

64. The total variance of Asset X is:

- 0.04
- 0.05
- 0.08
- 0.10

65. Which asset has higher R^2 in a CAPM regression?

- Asset Y
- Asset X
- Equal
- Cannot determine

66. [†] **[Select All That Apply]** Under CAPM, which statements are correct?

- ☐ Only systematic risk earns a risk premium
- ☐ Assets with negative beta can have expected returns below r_f
- ☐ Idiosyncratic risk increases expected return
- ☐ A zero-beta asset must have zero expected return

67. According to the CAPM, what should we expect for the intercept (α) in a time-series regression of any portfolio's excess return on the market's excess return?

- α equals zero.
- α equals the portfolio's mean excess return.
- α can be any value; CAPM makes no prediction about α .
- α equals the risk-free rate.

Questions 68–74: CAPM Regression Output

Reference Table: Time-series CAPM regressions

Portfolio	$\hat{\beta}$	Mean Excess	$\hat{\alpha}$	α t-stat	Vol	R^2
Small-Value	1.20	14%	4.0%	2.8	24%	0.60
Small-Growth	1.35	8%	−2.0%	−1.2	28%	0.55
Big-Value	0.90	11%	2.5%	2.1	18%	0.72
Big-Growth	1.05	10%	0.5%	0.4	16%	0.82
Market	1.00	9.5%	0.0%	—	16%	1.00

68. [†] **[Select All That Apply]** The Small-Value portfolio has $\alpha = 4.0\%$ with t-stat = 2.8. Which interpretations are valid?

- ☐ The CAPM perfectly explains Small-Value returns.
- ☐ Small-Value earns returns beyond what its market beta would predict.
- ☐ This is evidence against the CAPM or suggests missing risk factors.
- ☐ The high t-stat means Small-Value has lower total risk than average.

69. The correlation between Big-Growth and the market is approximately:

- 0.67
- Cannot be determined without additional data.
- 0.82
- 0.91

70. Small-Value has $\beta = 1.20$ and the market has expected excess return of 9.5%. Under the CAPM, Small-Value's expected excess return should be:

- 9.5%
- 10.0%
- 11.4%
- 14.0%

71. [†] **[Select All That Apply]** Which of the following reasons highlight the importance of the CAPM time-series regression?

- ☐ To estimate the asset's systematic risk exposure (β_i) and intercept (α_i).
 - ☐ To estimate the price of risk directly from the slope of the regression line.
 - ☐ To test the validity of the CAPM by examining if the intercept is statistically different from zero.
 - ☐ To determine the optimal risk-free rate to use for the period.
72. If the CAPM holds strictly true, what values should we expect for the intercept (α) and slope (β) in a time series regression using the tangency portfolio's returns?
- $\alpha = R_f, \beta = 1$
 - $\alpha = E[R_m], \beta = 0$
 - $\alpha = 0, \beta = 0$
 - $\alpha = 0, \beta = 1$
73. Which portfolio has the highest proportion of variance from idiosyncratic factors?
- Big-Growth
 - Big-Value
 - Small-Growth (lowest $R^2 = 0.55$)
 - Small-Value
74. If asset returns are normally distributed such that portfolios are fully characterized by mean and variance, what is the CAPM significance of the market portfolio?
- It serves as the Global Minimum Variance (GMV) portfolio.
 - It represents the portfolio with the highest possible absolute return.
 - It is the tangency portfolio, maximizing the Sharpe Ratio.
 - It lies on the inefficient portion of the frontier.

Section 8: DFA and Factor Investing (HW4)

Questions 75–79: Testing the CAPM

Background: DFA believes in factor premiums (size, value) beyond the market. The CAPM predicts that alpha should be zero if the market is the only priced factor.

75. [†] [Select All That Apply] Which methods can be used to test whether the CAPM holds?
- ☐ Check if time-series alphas are statistically different from zero.
 - ☐ Run a cross-sectional regression of mean returns on betas and check if intercept is zero.
 - ☐ Verify that all assets have the same Sharpe ratio as the market.
 - ☐ Confirm that all assets have the same expected return.
76. The cross-sectional regression of mean excess returns on betas gives an estimated “price of risk” $\hat{\lambda} = 7\%$. The market’s actual mean excess return is 9.5%. This suggests:
- The CAPM holds perfectly.
 - The estimated compensation per unit of beta is less than the market premium implies.
 - All portfolios have positive alpha.
 - The risk-free rate is incorrectly measured.
77. A portfolio has a CAPM regression alpha of 3% per year with a t-statistic of 2.5. Under the null hypothesis that CAPM holds, what should we conclude?
- The CAPM is confirmed because alpha is positive.
 - The positive alpha is statistically significant evidence against the CAPM for this portfolio.
 - The t-statistic is irrelevant; only the sign of alpha matters.
 - CAPM predicts alpha should be 3%, so this confirms the model.
78. A time-series CAPM regression for Stock Z yields $R^2 = 0.25$. A colleague concludes: “The CAPM fails because it only explains 25% of Stock Z’s return variation.” The best response is:
- Correct; $R^2 < 0.50$ means the CAPM is rejected.
 - Incorrect; CAPM is a model of expected returns, not of return variation. Low R^2 does not reject CAPM.
 - Incorrect; CAPM predicts $R^2 = 1$ for all assets.
 - Correct; low R^2 implies positive alpha.
79. A researcher finds that 3 out of 25 portfolios have statistically significant alphas (t-stat > 2.0). Another researcher argues this could be due to chance. The best response is:
- 3 out of 25 is definitely not due to chance.
 - With 25 tests at 5% level, we expect about 1-2 false positives by chance alone.
 - Multiple testing never creates false positives.
 - The t-statistic should be divided by 25 to account for multiple tests.

Section 9: Additional Questions

Questions 80–100: Mixed Topics

80. What is the Global Minimum Variance (GMV) portfolio?
- The portfolio that maximizes expected return without regard to risk
 - The portfolio with the minimum possible return
 - The portfolio with the lowest variance among all possible portfolios
 - The portfolio consisting solely of the risk-free asset
81. Which statistical property leads to “fat tails” in return distributions?
- High Mean.
 - High Variance.
 - Excess Kurtosis.
 - Low Variance.
82. When optimizing over **excess returns** (returns in excess of the risk-free rate), how do the optimal risky-asset weights differ from the case with no risk-free asset?
- The weights of risky assets must all be positive
 - The weights of risky assets no longer must sum to one
 - The Sharpe ratio of the tangency portfolio must increase
 - The weights are identical to the no-risk-free-asset case
83. In MVO, why is the covariance matrix often more reliably estimated than expected returns?
- Covariances are constant over time, whereas expected returns change.
 - Second moments (variances, covariances) converge faster with sample size than first moments (means).
 - Expected returns require daily data, while covariances can use monthly data.
 - Covariances are directly observable, while expected returns must be estimated.
84. A 24-month rolling window is used to estimate factor weights. After a regime shift, the replication will most likely:
- Adjust slowly and lag the new regime
 - Immediately match the new regime
 - Eliminate tracking error entirely
 - Become unrelated to the benchmark
85. A hedge ratio greater than 1 in a cross-hedge most likely occurs when:
- The hedge instrument is less volatile than the asset
 - The asset and hedge are perfectly negatively correlated

- The hedge instrument is more volatile than the asset
 - The hedge instrument is risk-free
86. Fund X has produced a very high Sharpe ratio over 3 years by grinding out small positive returns nearly every month. However, its return distribution shows significantly negative skewness and high kurtosis. What is the most likely interpretation?
- Fund X is skillful at managing risk
 - Fund X may be selling tail-risk (collecting premiums with rare large losses)
 - Fund X has a misreported Sharpe ratio
 - Fund X's strategy involves momentum trading
87. [†] **[Select All That Apply]** A replication shows high correlation but poor performance in a crisis. Which explanations are plausible?
- ☐ Model weights update with a lag
 - ☐ Factors fail to capture tail behavior
 - ☐ High correlation guarantees no drawdowns
 - ☐ Correlation implies identical returns
88. A portfolio's 5% VaR is -3% . If the portfolio is doubled in size (2x leverage), the new 5% VaR is approximately:
- -3%
 - -4.5%
 - -6%
 - -9%
89. In an EWMA volatility model, increasing λ (e.g., 0.94 to 0.97) will:
- Increase the weight on older observations
 - Increase the weight on the most recent observation
 - Eliminate volatility clustering
 - Make volatility constant
90. A portfolio has empirical 5% VaR = -2% and empirical 5% CVaR = -6% . This indicates:
- Severe tail losses relative to the VaR threshold
 - Near-normal tails
 - Low tail risk
 - Empirical VaR is overstated
91. A portfolio manager argues: "The historical Sharpe ratio is 0.40, so over a 25-year horizon, the probability of underperforming the risk-free rate is negligible." What is the approximate probability using the formula $P = \Phi(-\sqrt{h} \times \text{SR})$?
- 15%

- 5%
 - 2%
 - 0.5%
92. The volatility of **cumulative** returns over an h -year horizon (assuming i.i.d. returns) is:
- $\sigma \times \sqrt{h}$
 - σ/\sqrt{h}
 - $\sigma \times h$
 - σ/h
93. A portfolio has Sharpe ratio of 0.5 and Treynor ratio of 1.2. What can we infer?
- The portfolio has negative alpha.
 - The portfolio has substantial idiosyncratic (non-market) risk.
 - The portfolio's beta must be greater than 1.
 - The portfolio is perfectly correlated with the market.
94. If a fund has a high R^2 to the S&P 500, but a low beta, the CAPM would suggest that:
- The fund should have a higher expected return than the market.
 - The fund should have a lower expected return than the market.
 - The fund should have the same expected return as the market.
 - The fund's expected return cannot be determined from this information.
95. [†] [**Select All That Apply**] What should a CIO infer from 2013 performance (HDG 4.4% @ 4.8% vol vs S&P 32.4% @ 11% vol) for an alternatives allocation decision?
- ☐ HDG's "underperformance" in a bull year is irrelevant. Target role is diversification and drawdown mitigation, not beating pure equity beta in booms.
 - ☐ The relevant yardstick is HFRI / hedge-fund beta behavior. Replication is about risk shape and regime robustness.
 - ☐ Adding a sleeve like HDG can shift the portfolio efficient frontier even if it lags equities in a one-year bull.
 - ☐ Because 2013 was a bull, the only rational inference is that replication fails as an asset class.
96. What is the systematic volatility for an asset with $\beta = 0.6$ when market volatility is 15%?
- 3%
 - 6%
 - 9%
 - 15%
97. Equity return is normal with mean 6% and vol 10%. A bond returns a constant 6%. What is the approximate probability that equity underperforms bonds in one year?

- 10%
 - 25%
 - 50%
 - 75%
98. An investor uses the formula $P(\text{underperform}) = \Phi(-\sqrt{h} \times \text{SR})$ to calculate a 2% probability of stocks underperforming bonds over 25 years, based on a historical Sharpe ratio of 0.40. A colleague warns that the true Sharpe ratio might be 0.30. If the colleague is right, the actual probability of underperformance is approximately:
- Still 2% (the formula is robust to parameter uncertainty)
 - 5%
 - 7%
 - 15%
99. [†] **[Select All That Apply]** In a two-stage CAPM test, the first stage estimates each asset's beta from time-series regressions. The second stage regresses average excess returns on betas across assets. If the CAPM holds, which statements about the second-stage regression are correct?
- ☐ The intercept should be zero (or close to zero).
 - ☐ The slope should equal the market's average excess return.
 - ☐ The intercept should equal the risk-free rate.
 - ☐ The slope should equal zero if all assets are fairly priced.
100. A portfolio manager uses factor regression to decompose a fund's returns: $r_{fund} = \alpha + 0.8r_{Mkt} + 0.3r_{Bond} + \epsilon$. The fund has total volatility of 15%. If she hedges out both the market and bond exposures using short positions, what risk remains?
- Zero risk—the hedge eliminates all volatility.
 - Only market risk remains.
 - Idiosyncratic risk (the volatility of ϵ) remains.
 - The full 15% volatility remains unchanged.